$2.95 \AA, c=18.25 \AA$ and $Z=3$, in the hexagonal description (Hahn \& de Lorent, 1957). The hexagonal unit cell consists of three hexagonal sub-units, which are related to each other by the threefold screw axis parallel to the $c$ axis, as shown in Fig. 3. The dimensions of the sub-unit are $2.95 \AA$ along the $a$ axis, and $6.08 \AA$ along the $c$ axis. The structure of this sub-unit is quite similar to that of $\delta-\mathrm{AgFeO}_{2}$. The structures of $\mathrm{CuFeO}_{2}$ (Soller \& Thompson, 1935; Pabst, 1946) and $\mathrm{CuCrO}_{2}$ (Dannhauser \& Vaughan, 1955) are also analogous to that in $\mathrm{AgCrO}_{2}$.
Although the structure of $\alpha-\mathrm{AgFeO}_{2}$ has not been determined, we can build a model structure of it, in which three sub-units of $\mathrm{AgFeO}_{2}$ found in $\delta-\mathrm{AgFeO}_{2}$ are stacked along the $c$ axis in a similar fashion as in $\mathrm{AgCrO}_{2}$. The observed cell dimensions of $\alpha-\mathrm{AgFeO}_{2}$, $a=3.041$ and $c=18.55 \AA$ (Croft et al., 1964), are in good agreement with those of the model structure, $a=3.039$ and $c=18.59 \AA$.

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# The Structure of Octammine- $\mu$-amido- $\mu$-hydroxodicobalt Disulfate Dihydrate* 

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#### Abstract

The structures of two closely related compounds, octammine- $\mu$-amido- $\mu$-hydroxodicobalt disulfate dihydrate (the 'pure' compound) and the same compound with the hydroxo bridge partially substituted by chlorine (the 'mixed' compound), have been determined by X-ray diffraction techniques. The compounds form isostructural triclinic crystals: for the 'pure' compound, $a=9.066$ (4), $b=8.601$ (4), $c=$ 6.977 (3) $\AA, \alpha=106.92$ (3), $\beta=111.72$ (4), and $\gamma=68.62$ (4) ${ }^{\circ}$. The observed density is 1.86 (2) g.cm- ${ }^{-3}$ and that calculated for one formula weight in the unit cell is $1 \cdot 848$ (2) $\mathrm{g} . \mathrm{cm}^{-3}$. The space group is $P \overline{1}$; 1229 reflections were measured on a GE diffractometer and used to solve the structure. Refinement by full-matrix least-squares methods gave a final $R$ index of 0.027 . For the 'mixed' compound, $a=9.151$ (6), $b=8.633$ (6), $\mathrm{c}=6.910$ (3) $\AA, \alpha=106.66$ (7), $\beta=111.94$ (4), and $\gamma=68.95$ (9). The measured density is $1.88(2) \mathrm{g} . \mathrm{cm}^{-3}$ and the calculated density $1.853(2) \mathrm{g} . \mathrm{cm}^{-3}$. The structure was solved using 1106 reflections and refined to an $R$ index of 0.036 . In both compounds, the cation is disordered about a center of symmetry; bond distances and angles in the cation and the sulfate groups are normal.


## Introduction

The doubly-bridged dicobalt cation
$\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Co}<\underset{\mathrm{NH}_{2}}{\mathrm{OH}}>\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4}^{4^{+}}, \quad$ octammine- $\mu$-amido-

[^0]$\mu$-hydroxodicobalt ${ }^{4+}$, is obtained from Vortmann's (1885) sulfate and is a convenient starting material for the preparation of many other di-bridged dicobalt ions. The amide bridge is difficult to break, but the hydroxo bridge can be easily hydrolyzed, or substituted to give other di-bridged ions. The structure of this ion has not yet been reported. We intended to determine the structure several years ago, but instead of preparing the correct material, we made the $\mu$-amido, $\mu$-chloro compound (Barro, Marsh \& Schaefer, 1970). We have now
prepared two more compounds - including the one we wanted - and have determined their structures.

The octammine- $\mu$-amido- $\mu$-chlorodicobalt chloride we made earlier came from a concentrated hydrochloric acid reaction mixture. We wanted to determine the crystal structure of the $\mu$-amido, $\mu$-hydroxo compound with no bridging chloride: unfortunately, our first preparation had been once-recrystallized from dilute HCl and some Cl had become incorporated in the bridge. We found this out only after the structural analysis was nearly complete. We therefore began again, crystallizing our starting material from dilute sulfuric acid with no chloride present at all. We obtained well-formed crystals and again performed an X-ray structural analysis. We present the results of this in detail here, along with a brief description of the structure of the partially chloro-substituted salt. These two determinations, along with the earlier report on the fully substituted $\mu-\mathrm{NH}_{2}, \mu-\mathrm{Cl}$ compound (Barro et al., 1970), give a complete picture of structural changes with substitution at the bridging OH-group in these dicobalt compounds.

## Experimental

Vortmann's sulfate was prepared according to Werner's (1907) directions. The material was transformed to the nitrate, and the green $\mu-\mathrm{O}_{2}, \mu-\mathrm{NH}_{2}$ compound, $\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Co}<\mathrm{NH}_{2}>\mathrm{O}\left(\mathrm{NH}_{3}\right)_{4}\left(\mathrm{NO}_{3}\right)_{4}$ (Christoph, Marsh \& Schaefer, 1969), was removed by washing. The red nitrate which remained was used for the recrystallizations. The 'mixed' $\mathrm{NH}_{2},(\mathrm{OH}, \mathrm{Cl})$ bridged cation formed when 0.5 M HCl was used once in recrystallizing the powder; the pure $\mu-\mathrm{NH}_{2}, \mu-\mathrm{OH}$ compound was obtained by recrystallizing the starting material from $0.1 M \mathrm{H}_{2} \mathrm{SO}_{4}$.


(a)

(b)

(c)

Fig. 1. Representations of three dicobalt cations: (a) the Cl , $\mathrm{NH}_{2}$ bridged complex, ( $b$ ) the 'mixed' complex, and (c) the $\mathrm{OH}, \mathrm{NH}_{2}$ bridged complex. For the 'mixed' crystal (b), we were unable to determine realistic standard deviations for the bridging atoms. These occur so close together that simultaneous refinement was not possible. We have therefore reported these lengths to a hundredth of an ångström, and we believe the e.s.d.'s should be at least $\pm 0.04 \AA$ for each of these distances.

## The 'mixed' compound

Preliminary Weissenberg photographs indicated a triclinic cell. A sphere of average radius 0.075 (6) mm was ground from a larger chunk and carefully centered in a random orientation on the diffractometer. Unitcell dimensions were obtained from a least-squares fit of the $2 \theta$ values of 27 reflections; these and other crystal data are given in Table 1. A Delaunay (1933) reduction revealed no higher symmetry; the reduced cell had two angles greater than $120^{\circ}$, so the original cell was used for all further work. Data were collected on a Datexautomated GE diffractometer using cobalt $K \alpha$ radiation. All reflections within the $2 \theta$ range of 4 to $140^{\circ}$ were surveyed using a $\theta-2 \theta$ scan technique. The scan range varied from $2 \cdot 5^{\circ}$ at $20=12 \cdot 5^{\circ}$ to $3 \cdot 75^{\circ}$ at $2 \theta=120^{\circ}$

Table 1. Crystal data for the two compounds

and included both the $\alpha_{1}$ and $\alpha_{2}$ peaks. Background was counted for 60 seconds at both ends of the scan. Of the 1115 reflections scanned, 1106 were observed greater than background and were used in the solution and refinement of the structure. The data were corrected for background and for Lorentz and polarization factors; no correction for absorption was made because of the small value of $\mu R(0 \cdot 31)$. Standard deviations were assigned the measured intensities according to:

$$
\begin{gathered}
I=S-\left(B_{1}+B_{2}\right) \stackrel{t}{120} \\
\sigma(I)=\left[S+\left(B_{1}+B_{2}\right)\left(\frac{t}{120}\right)^{2}+(0 \cdot 02 S)^{2}\right]^{1 / 2}
\end{gathered}
$$

where $S$ is the scan count, $B_{1}$ and $B_{2}$ are background counts and $t$ is scan time. The additional term in $\sigma(I)$, $(0.02 S)^{2}$, is included to take account of errors other than those due to counting statistics (Busing \& Levy, 1957). During the initial data processing, the values of $\left.\langle | E\left\rangle,\langle | E^{2}\right|\right\rangle$, and $\langle | E^{2}-1| \rangle$ were calculated; these were, seriatim, $0.818,0.999$, and 0.917 , indicating that the space group has a center of symmetry and is thus No. 2, $P \overline{\mathrm{I}}$.
A three-dimensional Patterson map was calculated
from which the coordinates of the cobalt atom, one sulfur atom, and one bridging atom were obtained. There is one molecule of
$\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Co}(\mathrm{OH})\left(\mathrm{NH}_{2}\right) \mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4}\left(\mathrm{SO}_{4}\right)_{2} .2 \mathrm{H}_{2} \mathrm{O}$ in the unit cell, or half a molecule in the asymmetric unit; therefore the bridging groups have to be disordered if the space group is to be $P \overline{1}$. Successive electron density maps and structure factor calculations located the rest of the nonhydrogen atoms in the structure. Full-matrix least-squares refinement converged with an $R$ index of 0.081 ; at this stage, the bridging atoms were considered to be an oxygen atom and a nitrogen atom. The hydrogen atoms of the ammine groups were then added, their coordinates being taken from difference maps calculated in the planes where they were expected. Four cycles of least-squares calculations, varying the positional and thermal parameters of all the atoms (hydrogen atoms isotropic, others anisotropic), a scale factor, and a secondary extinction factor (Larson, 1967), gave an $R$ index of 0.043 . However, one of the bridging atoms, assumed to be an oxygen atom, was $2 \cdot 23 \AA$ from the cobalt atom. This distance is much too long to be a $\mathrm{Co}-\mathrm{O}$ bond. Since such a distance is appropriate for a $\mathrm{Co}-\mathrm{Cl}$ bond, and since there were positive regions of electron density remaining around this atom, we began to try various combinations of Cl and

Table 2. Positional, thermal, and population parameters of the heavy atoms
All positional and anisotropic thermal parameters have been multiplied by $10^{4}$. Anisotropic temperature factors are of the form:

|  | $x$ | $y$ | $z$ | $\begin{array}{r} B \text { or } \\ b_{11} \end{array}$ | $b_{22}$ | $b_{33}$ | $b_{12}$ | $b_{13}$ | $b_{23}$ | Population* |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) The 'mixed' compound |  |  |  |  |  |  |  |  |  |  |
| Co | 6727 (0.9) | 3808 (0.9) | 5374 (1) | 51 (2) | 65 (2) | 128 (3) | -40 (2) | 37 (3) | 26 (3) |  |
| $\mathrm{N}(1)$ | 5889 (6) | 1824 (6) | 4232 (8) | 55 (7) | 61 (8) | 170 (15) | -26 (13) | 51 (18) | 16 (16) |  |
| $\mathrm{N}(2)$ | 7739 (6) | 5656 (6) | 6514 (8) | 47 (8) | 82 (8) | 150 (14) | -40 (13) | 35 (16) | 16 (18) |  |
| $\mathrm{N}(3)$ | 8317 (6) | 2754 (8) | 7811 (8) | 90 (9) | 108 (9) | 151 (14) | -88 (15) | 33 (17) | 92 (21) |  |
| N(4) | 8206 (6) | 2839 (7) | 3599 (8) | 68 (8) | 109 (9) | 155 (13) | -37 (14) | 63 (17) | 35 (19) |  |
| N (5) | 4957 (9) | 4998 (9) | 3250 (13) | $2 \cdot 21$ (14) |  |  |  |  |  | 0.5 |
| Cl | 4937 (23) | 5049 (20) | 2365 (16) | 598 (54) | 405 (42) | -11 (22) | -915 (88) | 163 (52) | -96(44) | 0.107 |
| $\mathrm{O}(1)$ | 4955 (8) | 5015 (8) | 3179 (11) | $2 \cdot 28$ (20) |  |  |  |  |  | 0.393 |
| S | 2439 (1) | 2531 (2) | 7844 (2) | 54 (2) | 70 (2) | 135 (4) | -16(3) | 44 (4) | 51 (4) |  |
| O(2) | 3283 (5) | 2091 (5) | 9955 (6) | 144 (7) | 132 (8) | 128 (10) | -29 (12) | 30 (14) | 93 (14) |  |
| $\mathrm{O}(3)$ | 1402 (4) | 4295 (5) | 7991 (6) | 78 (6) | 72 (6) | 271 (12) | 8 (10) | 80 (14) | 75 (14) |  |
| O(4) | 1425 (5) | 1392 (5) | 6564 (7) | 75 (6) | 105 (8) | 345 (14) | - 50 (11) | 24 (15) | -17 (16) |  |
| $\mathrm{O}(5)$ | 3689 (5) | 2305 (5) | 6863 (7) | 106 (7) | 171 (8) | 285 (13) | 16 (12) | 210 (16) | 191 (17) |  |
| O(6) | 6923 (5) | 838 (5) | 9296 (6) | 99 (7) | 134 (8) | 243 (12) | -87 (12) | 47 (14) | 143 (15) |  |
| (b) The 'pure' compound |  |  |  |  |  |  |  |  |  |  |
| Co | 6692 (0.5) | 3834 (0.5) | 5354 (0.6) | 55 (1) | 60 (1) | 112 (1) | -26 (1) | 52 (2) | 28 (1) |  |
| N(1) | 5870 (3) | 1837 (3) | 4192 (4) | 68 (4) | 64 (4) | 159 (7) | -31(7) | 62 (9) | 25 (8) |  |
| N(2) | 7730 (3) | 5672 (3) | 6525 (4) | 68 (5) | 73 (4) | 116 (6) | -41 (7) | 58 (8) | 22 (9) |  |
| N(3) | 8293 (3) | 2760 (4) | 7769 (4) | 73 (4) | 96 (4) | 158 (7) | -42 (7) | 37 (9) | 104 (10) |  |
| $\mathrm{N}(4)$ | 8208 (3) | 2845 (4) | 3610 (4) | 64 (4) | 90 (4) | 136 (7) | -37 (7) | 59 (8) | 9 (10) |  |
| N(5) | 4944 (20) | 5034 (21) | 3111 (27) | 1.78 (48) |  |  |  |  |  | 0.5 |
| $\mathrm{O}(1)$ | 4971 (16) | 4976 (17) | 3250 (20) | $1 \cdot 38$ (42) |  |  |  |  |  | $0 \cdot 5$ |
| S | 2456 (0.8) | 2564 (0.8) | 7865 (1) | 64 (1) | 70 (1) | 128 (2) | -24(2) | 57 (2) | 47 (2) |  |
| $\mathrm{O}(2)$ | 3252 (3) | 2092 (3) | 9955 (3) | 159 (4) | 123 (4) | 131 (5) | -67 (7) | 49 (8) | 78 (7) |  |
| $\mathrm{O}(3)$ | 1410 (3) | 4339 (3) | 8028 (4) | 105 (4) | 75 (3) | 279 (7) | 5 (6) | 108 (8) | 74 (8) |  |
| O(4) | 1454 (3) | 1422 (3) | 6524 (4) | 75 (3) | 104 (4) | 242 (6) | -56 (6) | 22 (8) | -8 (8) |  |
| O (5) | 3764 (3) | 2350 (3) | 6966 (4) | 110 (4) | 156 (4) | 288 (7) | -29 (7) | 206 (9) | 176 (9) |  |
| O(6) | 6993 (3) | 823 (3) | 9341 (4) | 98 (4) | 135 (5) | 317 (8) | -82 (7) | 40 (9) | 195 (10) |  |

[^1]Table 3. Positional, thermal, and population parameters of the hydrogen atoms
All positional parameters have been multiplied by 103 .

|  | $x$ | $y$ | $z$ | $B\left(\AA^{2}\right)$ | Popu lation |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (a) The 'mixed' compound |  |  |  |  |  |
| $\mathrm{H}(1)$ | 530 (7) | 183 (7) | 291 (10) | $3 \cdot 0$ (13) |  |
| $\mathrm{H}(2)$ | 518 (8) | 172 (7) | 480 (9) | $3 \cdot 0$ (13) |  |
| H(3) | 677 (9) | 88 (8) | 413 (9) | $4 \cdot 5$ (14) |  |
| H(4) | 751 (8) | 621 (8) | 762 (10) | $3 \cdot 1$ (15) |  |
| $\mathrm{H}(5)$ | 864 (8) | 517 (8) | 673 (9) | $0 \cdot 4$ (15) |  |
| H (6) | 728 (8) | 642 (8) | 535 (11) | $3 \cdot 9$ (14) |  |
| H(7) | 827 (8) | 352 (9) | 887 (10) | $4 \cdot 2$ (17) |  |
| H (8) | 803 (7) | 205 (8) | 797 (9) | $2 \cdot 9$ (15) |  |
| $\mathrm{H}(9)$ | 933 (8) | 208 (8) | 732 (9) | $2 \cdot 8$ (13) |  |
| $\mathrm{H}(10)$ | 903 (8) | 224 (7) | 422 (9) | $2 \cdot 0$ (13) |  |
| $\mathrm{H}(11)$ | 827 (8) | 378 (9) | 292 (10) | $5 \cdot 4$ (16) |  |
| $\mathrm{H}(12)$ | 785 (10) | 207 (11) | 211 (13) | $6 \cdot 3$ (21) |  |
| $\mathrm{H}(13)$ | 539 (-) | 599 (-) | 317 (-) | $4 \cdot 0$ (-) | 0.683 |
| H (14) | 452 (-) | 409 (-) | 211 (-) | $4 \cdot 0$ (-) | $0 \cdot 683$ |
| [ $\mathrm{H}(15)$ and $\mathrm{H}(16)$, attached to the water oxygen atom, were notassigned.] |  |  |  |  |  |

(b) The 'pure' compound

| $\mathrm{H}(1)$ | 520 (4) | 185 (4) | 278 (5) | $2 \cdot 5$ (6) |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}(2)$ | 532 (4) | 168 (4) | 479 (5) | $2 \cdot 6$ (7) |  |
| H(3) | 666 (5) | 85 (5) | 427 (5) | $3 \cdot 6$ (8) |  |
| H(4) | 755 (4) | 626 (4) | 758 (5) | $2 \cdot 1$ (7) |  |
| H(5) | 879 (5) | 520 (4) | 688 (5) | $2 \cdot 6$ (7) |  |
| H(6) | 746 (4) | 629 (5) | 571 (6) | $3 \cdot 3$ (8) |  |
| H(7) | 837 (5) | 351 (5) | 885 (6) | $4 \cdot 2$ (9) |  |
| H(8) | 800 (4) | 206 (4) | 806 (5) | $3 \cdot 0$ (8) |  |
| H(9) | 936 (5) | 220 (5) | 760 (6) | $4 \cdot 5$ (8) |  |
| $\mathrm{H}(10)$ | 925 (5) | 233 (4) | 429 (5) | $3 \cdot 2$ (7) |  |
| H(11) | 836 (4) | 365 (5) | 324 (5) | $4 \cdot 0$ (9) |  |
| H(12) | 787 (4) | 221 (4) | 264 (6) | $2 \cdot 4$ (8) |  |
| H(13) | 524 (6) | 568 (6) | 279 (7) | $3 \cdot 1$ | 0.750 |
| H(14) | 471 (5) | 440 (6) | 211 (7) | $3 \cdot 1$ | 0.750 |
| H(15) | 703 (4) | 995 (4) | 949 (5) | $3 \cdot 1$ |  |
| H(16) | 615 (4) | 120 (5) | 891 (6) | $3 \cdot 1$ |  |

Table 4. Supplementary bond distances and bond angles

|  | 'Mixed' | 'Pure' |
| :--- | :---: | :---: |
| $\mathrm{N}(1)-\mathrm{H}(1)$ | $0.87 \AA$ | $0.95 \AA$ |
| $\mathrm{~N}(1)-\mathrm{H}(2)$ | 0.92 | 0.83 |
| $\mathrm{~N}(1)-\mathrm{H}(3)$ | 0.93 | 0.89 |
| $\mathrm{~N}(2)-\mathrm{H}(4)$ | 0.83 | 0.80 |
| $\mathrm{~N}(2)-\mathrm{H}(5)$ | 0.76 | 0.87 |
| $\mathrm{~N}(2)-\mathrm{H}(6)$ | 1.06 | 0.80 |
| $\mathrm{~N}(3)-\mathrm{H}(7)$ | 0.84 | 0.84 |
| $\mathrm{~N}(3)-\mathrm{H}(8)$ | 0.80 | 0.84 |
| $\mathrm{~N}(3)-\mathrm{H}(9)$ | 1.02 | 0.95 |
| $\mathrm{~N}(4)-\mathrm{H}(10)$ | 0.79 | 0.90 |
| $\mathrm{~N}(4)-\mathrm{H}(11)$ | 1.08 | 0.87 |
| $\mathrm{~N}(4)-\mathrm{H}(12)$ | 1.06 | 0.78 |
| $\mathrm{~N}(5)-\mathrm{H}(3)$ | 1.09 | 0.81 |
| $\mathrm{~N}(5)-\mathrm{H}(14)$ | 1.01 | 0.77 |
| $\mathrm{O}(6)-\mathrm{H}(15)$ | - | 0.77 |
| $\mathrm{O}(6)-\mathrm{H}(16)$ | - | 0.69 |
| $\mathrm{~S}-\mathrm{O}(2)$ | $1.460(4)$ | $1.472(2)$ |
| $\mathrm{S}-\mathrm{O}(3)$ | $1.475(4)$ | $1.472(2)$ |
| $\mathrm{S}-\mathrm{O}(4)$ | $1.467(5)$ | $1.467(3)$ |
| $\mathrm{S}-\mathrm{O}(5)$ | $1.466(5)$ | $1.468(3)$ |
| $\mathrm{Co}-\mathrm{Co}$ |  | $3.035(1)$ |
|  |  | $2.941(1)$ |


|  | 'Mixed' | 'Pure' |
| :---: | :---: | :---: |
| $\mathrm{N}(1)-\mathrm{Co}-\mathrm{N}(2)$ | 175.4 (2) ${ }^{\circ}$ | 174.4 (1) ${ }^{\circ}$ |
| $\mathrm{N}(1)-\mathrm{Co}-\mathrm{N}(3)$ | $90 \cdot 0$ (2) | 89.9 (1) |
| $\mathrm{N}(1)-\mathrm{Co}-\mathrm{N}(4)$ | 89.8 (2) | 89.1 (1) |
| $\mathrm{N}(1)-\mathrm{Co}-\mathrm{N}(5)$ | $90 \cdot 5$ (4) | $92 \cdot 3$ (6) |
| $\mathrm{N}(1)-\mathrm{Co}-\mathrm{O}(1)$ | $90 \cdot 8$ (5) | 90.0 (5) |
| $\mathrm{N}(1)-\mathrm{Co}-\mathrm{Cl}$ | 91.0 (5) | (5) |
| $\mathrm{N}(2)-\mathrm{Co}-\mathrm{N}(3)$ | $87 \cdot 4$ (2) | $86 \cdot 7$ (1) |
| $\mathrm{N}(2)-\mathrm{Co}-\mathrm{N}(4)$ | 86.7 (2) | 86.6 (1) |
| $\mathrm{N}(2)-\mathrm{Co}-\mathrm{N}(5)$ | 92.7 (4) | 92.3 (6) |
| $\mathrm{N}(2)-\mathrm{Co}-\mathrm{O}(1)$ | 92.3 (3) | 93.9 (5) |
| $\mathrm{N}(2)-\mathrm{Co}-\mathrm{Cl}$ | 91.4 (5) |  |
| $\mathrm{N}(3)-\mathrm{Co}-\mathrm{N}(4)$ | $94 \cdot 7$ (2) | $94 \cdot 4$ (1) |
| $\mathrm{N}(3)-\mathrm{Co}-\mathrm{N}(5)$ | 171.4 (5) | $174 \cdot 4$ (5) |
| $\mathrm{N}(3)-\mathrm{Co}-\mathrm{O}(1)$ | $172 \cdot 5$ (3) | $172 \cdot 7$ (5) |
| $\mathrm{N}(3)-\mathrm{Co}-\mathrm{Cl}$ | 176.8 (5) | - |
| $\mathrm{N}(4)-\mathrm{Co}-\mathrm{N}(5)$ | 93.9 (5) | $91 \cdot 2$ (5) |
| $\mathrm{N}(4)-\mathrm{Co}-\mathrm{O}(1)$ | 92.8 (3) | $92 \cdot 9$ (5) |
| $\mathrm{N}(4)-\mathrm{Co}-\mathrm{Cl}$ | 82.3 (5) | 92, |
| $\mathrm{N}\left(5^{\prime}\right)-\mathrm{Co}-\mathrm{O}(1)$ | $77 \cdot 7$ (5) | 81.2 (7) |
| $\mathrm{N}\left(5^{\prime}\right)-\mathrm{Co}-\mathrm{Cl}$ | 88.0 (6) |  |
| $\mathrm{O}(1)-\mathrm{Co}-\mathrm{Cl}$ | $10 \cdot 5$ (5) |  |
| $\mathrm{Co}-\mathrm{N}(5)-\mathrm{Co}^{\prime}$ | $103 \cdot 6$ (6) | 96.6 (8) |
| $\mathrm{Co}-\mathrm{O}(1)-\mathrm{Co}^{\prime}$ | $101 \cdot 2$ (3) | $101 \cdot 2$ (6) |
| $\mathrm{Co}-\mathrm{Cl}--\mathrm{Co}^{\prime}$ | 79.9 (4) |  |
| $\mathrm{O}(2)-\mathrm{S}-\mathrm{O}(3)$ | $110 \cdot 3$ (2) | $110 \cdot 3$ (1) |
| $\mathrm{O}(2)-\mathrm{S}-\mathrm{O}(4)$ | $109 \cdot 2$ (3) | 108.8 (1) |
| $\mathrm{O}(2)-\mathrm{S}-\mathrm{O}(5)$ | 108.0 (3) | 108.2 (2) |
| $\mathrm{O}(3)-\mathrm{S}-\mathrm{O}(4)$ | $110 \cdot 1$ (3) | 110.4 (1) |
| $\mathrm{O}(3)-\mathrm{S}-\mathrm{O}(5)$ | 110.0 (3) | 110.0 (1) |
| $\mathrm{O}(4)-\mathrm{S}-\mathrm{O}(5)$ | $109 \cdot 2$ (3) | 109.0 (1) |
| $\mathrm{Co}-\mathrm{N}(1)-\mathrm{H}(1)$ | 110 | 111 |
| $\mathrm{Co}-\mathrm{N}(1)-\mathrm{H}(2)$ | 119 | 118 |
| $\mathrm{Co}-\mathrm{N}(1)-\mathrm{H}(3)$ | 108 | 114 |
| $\mathrm{H}(1)-\mathrm{N}(1)-\mathrm{H}(2)$ | 101 | 106 |
| $\mathrm{H}(1)-\mathrm{N}(1)-\mathrm{H}(3)$ | 102 | 109 |
| $\mathrm{H}(2)-\mathrm{N}(1)-\mathrm{H}(3)$ | 115 | 98 |
| $\mathrm{Co}-\mathrm{N}(2)-\mathrm{H}(4)$ | 110 | 115 |
| $\mathrm{Co}-\mathrm{N}(2)-\mathrm{H}(5)$ | 101 | 108 |
| $\mathrm{Co}-\mathrm{N}(2)-\mathrm{H}(6)$ | 108 | 112 |
| $\mathrm{H}(4)-\mathrm{N}(2)-\mathrm{H}(5)$ | 112 | 105 |
| $\mathrm{H}(4)-\mathrm{N}(2)-\mathrm{H}(6)$ | 111 | 107 |
| $\mathrm{H}(5)-\mathrm{N}(2)-\mathrm{H}(6)$ | 115 | 111 |
| $\mathrm{Co}-\mathrm{N}(3)-\mathrm{H}(7)$ | 105 | 109 |
| $\mathrm{Co}-\mathrm{N}(3)-\mathrm{H}(8)$ | 111 | 115 |
| $\mathrm{Co}-\mathrm{-N}(3)-\mathrm{H}(9)$ | 104 | 113 |
| $\mathrm{H}(7)-\mathrm{N}(3)-\mathrm{H}(8)$ | 106 | 104 |
| $\mathrm{H}(7)-\mathrm{N}(3)-\mathrm{H}(9)$ | 127 | 109 |
| $\mathrm{H}(8)-\mathrm{N}(3)-\mathrm{H}(9)$ | 103 | 107 |
| $\mathrm{Co}-\mathrm{N}(4)-\mathrm{H}(10)$ | 108 | 115 |
| $\mathrm{Co}-\mathrm{N}(4)-\mathrm{H}(11)$ | 112 | 110 |
| $\mathrm{Co}-\mathrm{N}(4)-\mathrm{H}(12)$ | 120 | 110 |
| $\mathrm{H}(10)-\mathrm{N}(4)-\mathrm{H}(11)$ | 119 | 101 |
| $\mathrm{H}(10)-\mathrm{N}(4)-\mathrm{H}(12)$ | 103 | 109 |
| $\mathrm{H}(11)-\mathrm{N}(4)-\mathrm{H}(12)$ | 93 | 112 |
| $\mathrm{Co}-\mathrm{N}(5)-\mathrm{H}(13)$ | 105 | 114 |
| $\mathrm{Co}-\mathrm{N}(5)-\mathrm{H}(14)$ | 105 | 117 |
| $\mathrm{Co}^{\prime}-\mathrm{N}(5)-\mathrm{H}(13)$ | 104 | 113 |
| $\mathrm{Co}^{\prime}-\mathrm{N}(5)-\mathrm{H}(14)$ | 105 | 111 |
| $\mathrm{H}(13)-\mathrm{N}(5)-\mathrm{H}(14)$ | 131 | 106 |
| $\mathrm{H}(15)-\mathrm{O}(6)-\mathrm{H}(16)$ | - | 104 |

An approximate e.s.d. of an N-H bond length would be $0.1 \AA$; for a bond angle involving $\mathrm{H}: 2-3^{\circ}$.

O atoms to explain the electron density in this region. We represented the bridging groups as a nitrogen atom with population one, and a combination of a chlorine atom and an oxygen atom whose populations summed to one. Refinement of our final model by the least-
squares method led to an $R$ index of 0.036 . The ratio of chlorine to oxygen atoms in the bridge turned out to be $21: 79$. The parameters obtained from the refinement are given in Tables 2 and 3; the estimated standard deviations listed there are underestimated, because the final cycles were block diagonal rather than full matrix. A drawing of the cation is given in Fig. 1(b), and supplementary bond distances and angles are listed in Table 4.

Some of the thermal parameters in Tables 2 and 3 deserve comment. The $B$ 's of the hydrogen atoms range from 0.39 to $6.29 \AA$, but do not differ significantly from an average value of about $3 \cdot 5 \AA^{2}$. The thermal parameters of the bridging Cl atom are very large and are nonpositive definite, i.e. physically unreal. The problem is caused by the nearness of the bridging N and $O$ atoms and by the very strong coupling between the thermal and population parameters of these atoms.

Because this crystal obviously contained some chloride in the bridging groups, we decided to discontinue further work and to prepare the pure material. However, since the data were of high quality, it seemed appropriate to report these results in the present abbreviated form.

## The 'pure' compound

Well-formed red crystals were obtained from $0 \cdot 1 \mathrm{M}$ $\mathrm{H}_{2} \mathrm{SO}_{4}$. Weissenberg and rotation photographs showed about the same triclinic cell as found for the mixed compound. A nearly cubic crystal was found, with sides of 0.19 mm . This crystal was mounted (again in a random orientation), carefully centered on the diffractometer, and cell dimensions measured. These are given, along with the other crystal data, in Table 1. The cell dimensions are, of course, nearly the same as for the mixed compound; the shortening of $a$ and $b$

Table 5. The 'pure' compound
The columns contain, in order, $l, 10 F_{\text {obs }}$, and $10 F_{\text {calc }}$ on an absolute scale.




$\begin{array}{lll}-2 & 196 \\ -1 & 121 & = \\ & 1 & 0\end{array}$
 $\begin{array}{ccc}3 & 47 & -46 \\ 6 & 6 & 4 \\ 6 & 246 & 243 \\ 1 & 100 & 1107 \\ 2 & 215 & 21 \\ 3 & 10 & -19\end{array}$ $\begin{array}{cccc}1 & -2 & 2 & -1 \\ 1 & 19 & 20 & 1\end{array}$ 4

reflects the shorter Co-Co distance in the 'pure' compound. Data were collected using Fe foil-filtered cobalt radiation and a $\theta-2 \theta$ scan technique. The scan range varied from $2 \cdot 2^{\circ}$ at $2 \theta=30^{\circ}$ to $3 \cdot 2^{\circ}$ at $2 \theta=110^{\circ}$. Background was counted for 30 seconds at each end of the
scan. Three standard reflections ( $\overline{561}, 570$, and $\overline{7} 01$ ) were followed throughout the data collection. Their intensities showed no variations greater than those expected from counting statistics. The intensities and their standard deviations were obtained from the

Table 6. The 'mixed' compound
The columns contain, in order, $h, 10 F_{\text {obs }}$, and $10 F_{\text {calc }}$ on an absolute scale.


Table 7. The hydrogen bonding system ('pure' compound)

measured counts as described above. At the end of the data collection, all reflections which had given negative values for the intensity were remeasured, along with a number for which there were obvious errors in the data. In addition, all extremely strong reflections were remeasured with the tube current reduced sufficiently to ensure that the counting rate would never exceed the capacity of the system. All the reflections were put on a common scale by means of the check reflections and merged to give a data set of 1229 observed reflections (out of 1235 measured) which were used in the solution and refinement of the structure. Lorentz and polarization corrections were made, but no absorption corrections were considered necessary, as $\mu$ for this compound is $39.84 \mathrm{~cm}^{-1}$ and thus $\mu R_{\text {avg }}=0.52$. This neglect could have led to maximum errors of about $4 \%$ in the structure factors. The structure was solved independently of the first one; solution and refinement followed essentially the same course. After all heavy atoms had been located, their positional and anisotropic thermal parameters were refined by full-matrix leastsquares methods to an $R$ index of $0 \cdot 036$. Difference maps were calculated in the planes where the ammine hydrogen atoms were expected, and these were located; their positions and isotropic temperature factors were then refined. Several cycles of refinement, including a single scale factor, positional parameters for all atoms, isotropic thermal parameters for the disordered bridging nitrogen and oxygen atoms, and anisotropic thermal parameters for the rest of the heavy atoms (all arranged in several matrices) converged with an $R$ index of 0.029 ; the goodness-of-fit was $2 \cdot 59$. The addition of a secondary extinction factor reduced $R$ to 0.027 and lowered the goodness-of-fit to 2.52 . In the final three cycles of refinement, 136 parameters were varied in a single matrix: positional and anisotropic thermal parameters for the cobalt and nonbridging ligand atoms, positional and isotropic thermal parameters for the bridging oxygen and nitrogen atoms and the hydrogen atoms, a single scale factor, and a secondary extinction factor (Larson, 1967). The final parameters are listed in Tables 2 and 3; the cation is depicted in Fig. $1(b)$, and supplementary bond distances are given in Table 4.

We represented the disorder in the cation by giving the bridging atoms population factors of $0 \cdot 5$. A difference map in the plane where the hydrogen atoms of the bridging N and O atoms were expected clearly showed two areas of significant electron density ( $\sim 0 \cdot 5-0.6$ e. $\AA^{-3}$ ). We assumed that the hydroxyl hydrogen atom was equally distributed between these two positions and that it coincided with the ammine hydrogen atoms. Therefore, each of these two positions was assigned a total H -atom population of 0.75 .

The observed and calculated structure factors for both structure determinations are given in Tables 5 and 6. All calculations were done on an IBM 360/75 computer, using the programs of the CRYM X-ray computing system; form factors for hydrogen atoms were
taken from Stewart, Davidson \& Simpson (1965) and those for the heavy atoms from International Tables for X-ray Crystallography (1962). Anomalous dispersion corrections were made by subtracting $2 \cdot 19 \mathrm{e}$, from the curve for cobalt and adding 0.34 e to the curve for sulfur (Cromer, 1965); $\Delta f^{\prime \prime}$ was ignored.

## Description of the structure

## The cation

Fig. $1(b)$ and ( $c$ ) shows the cations of these compounds. The bond distances and angles are normal and are quite comparable to those found in the $\mu-\mathrm{Cl}$, $\mathrm{NH}_{2}$-dicobalt cation (Barro et al., 1970), shown in Fig. 1(a). All three of these compounds have been refined to low values of the $R$ index; the e.s.d.'s in the individual bond lengths are also all quite small. The out-of-plane cobalt-nitrogen distances average $1.957 \AA$, with an r.m.s. deviation from the mean of $0.005 \AA$. This agreement is as good as one could expect, and probably indicates that all six measurements are of chemically identical bonds. The in-plane cobalt-nitrogen bonds may, however, show the influence of the differing ligands ( $\mathrm{Cl}, \mathrm{O}$, or N ) trans to them. They average $1.964 \AA$, insignificantly different from the out-of-plane average, but the r.m.s. deviation from the mean is $0.011 \AA$, rather larger than the individual e.s.d.'s would predict. The two in-plane distances in the 'pure' $\mu$ - $\mathrm{OH}, \mu-\mathrm{NH}_{2}$ compound differ by so much, however $(0.010 \AA)$, that we are unable to offer any consistent explanation of these variations.
The situation with respect to the bridging groups is a bit less satisfactory. In all three compounds the cation crystallizes at a center of symmetry, requiring the bridging ligands to be disordered.* In the compounds with a chloro-bridge, the heavy chlorine atom obscures to some extent the lighter bridging atom; even for the $\mu-\mathrm{OH}, \mu-\mathrm{NH}_{2}$ compound, the data are not sufficiently precise to permit us to distinguish a half-nitrogen atom from a half-oxygen atom. In all cases, the chemical species were assigned so as to give chemically reasonable bond lengths. Thus, the region of electron density 1.893 and $1.911 \AA$ from the cobalt atoms in the $\mu-\mathrm{OH}$, $\mu-\mathrm{NH}_{2}$ compound was called an oxygen atom; our identification of it as such is based on chemical reasoning and not on the X-ray evidence. Note that the

[^2]disordered half-atoms in the bridge of the $\mu-\mathrm{OH}$, $\mu-\mathrm{NH}_{2}$ compound are only $0.11 \AA$ apart. During the early part of our work, we tried to include both of these atoms (positional parameters and isotropic temperature factors) in the refinement as part of a large matrix, but the refinement diverged. At the end of the refinement, when all other shifts were small ( $R=0.027$ ), we tried this again and found that the refinement converged. The same technique may work in other refinements with nearly singular matrices.

## The sulfate groups

Each structure contains one independent sulfate group, and in each case the geometry is thoroughly satisfactory. The hydrogen-bonding to the sulfate groups does not distort either of the groups significantly, but both are held in the structure firmly enough so that their thermal motions are not extreme. The eight separate measurements of the S-O bond distance give $1.468 \AA$ (standard deviation from the mean 0.004 $\AA$ ). In a study of five different sulfates, Baur (1964) found 1.473 (1) $\AA$ for the S-O distance; thus, our results agree very well with those he considered. The average deviation of all the O-S-O angles from $109 \cdot 5$ is $0 \cdot 8^{\circ}$, indicating the sulfate ions are almost regular tetrahedra.

## The hydrogen bonding

The hydrogen-bonding scheme we propose for this compound is outlined in Table 7. All but one hydrogen atom of the coordinated ammine groups and both hydrogen atoms of the water molecule are involved in hydrogen bonds. Each oxygen atom of the sulfate group accepts at least one hydrogen bond and the water molecule accepts two, although none of these hydrogen bonds is very strong. Thus the entire crystal is held together by this extensive network of hydrogen bonds. Some of the $\mathrm{N}-\mathrm{H} \cdots \mathrm{O}$ distances are as long as $3 \cdot 13 \AA$, indicating fairly weak interactions. Perhaps because of the disorder in the cation, or perhaps because of crowding, we are able to identify only one H -bonding contact involving the bridging atoms: this is a $2.91 \AA$ distance between $\mathrm{O}(1)$ of the sulfate group and either the -OH or the $-\mathrm{NH}_{2}$ bridging group.

## The thermal motion

Overall, the thermal motion in this compound appears to be relatively small. Anisotropic motions are present but they correspond in general to physically reasonable models, with major axes of vibration gen-
erally perpendicular to chemical bonds. Table 8 lists the r.m.s. displacements along the three principal axes of the derived thermal ellipsoids for the heavy atoms. The bridging atoms show rather small temperature factors [ 1.78 and $1.38 \AA^{2}$ for $\mathrm{N}(5)$ and $\mathrm{O}(1)$ ], and the isotropic temperature factors of the hydrogen atoms are not much larger ( $2 \cdot 14$ to $4 \cdot 46 \AA^{2}$ ). The oxygen atom of the water molecule exhibits the largest motion of any in the structure, which is not surprising since it is the least strongly bonded atom.

Table 8. R.m.s. displacements of atoms along the principal axes of their thermal ellipsoids ('pure' compound)

| Co | $0.017,0.020,0.023 \AA$ |
| :--- | :--- |
| $\mathrm{~N}(1)$ | $0.020,0.024,0.034$ |
| $\mathrm{~N}(2)$ | $0.021,0.022,0.025$ |
| $\mathrm{~N}(3)$ | $0.022,0.026,0.038$ |
| $\mathrm{~N}(4)$ | $0.021,0.025,0.035$ |
| S | $0.020,0.024,0.027$ |
| $\mathrm{O}(2)$ | $0.025,0.039,0.058$ |
| $\mathrm{O}(3)$ | $0.020,0.043,0.059$ |
| $\mathrm{O}(4)$ | $0.023,0.031,0.066$ |
| $\mathrm{O}(5)$ | $0.021,0.040,0.071$ |
| $\mathrm{O}(6)$ | $0.029,0.033,0.073$ |

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[^0]:    * Contribution No. 4341 from the Arthur Amos Noyes Laboratory of Chemical Physics, California Institute of Technology, Pasadena, California 91109 , U.S.A.

[^1]:    * Unless a number is given here, the population was $1 \cdot 0$.

[^2]:    * Even if the bridging groups are ordered, leading to the space group $P 1$, the departures from a centric structure must be extremely small. The data, although of high quality, almost certainly cannot distinguish between the two cases. Structure factors calculated for an ordered structure would show phase angles slightly different from 0 or $\pi$, but their magnitudes would differ only trivially from those calculated for our disordered model. Least-squares refinement of the ordered structure would surely be catastrophic, because of near-singularities in many parameter matrices. Finally, there is no hint in the temperature factors of the nonbridging atoms of any molecular distortion that might suggest significant departure from the centric structure. All of these considerations lead us to conclude that the structure as determined here is appropriately described as disordered.

